



Electron emission and backscattering from surfaces⁺

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⁺ Funded by DFG under contract 495729137

Outline



1. Motivation

2. Computational approach

3. Numerical results

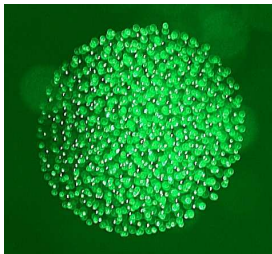
4. Conclusion

Motivation

Secondary electron emission – Why should we care?

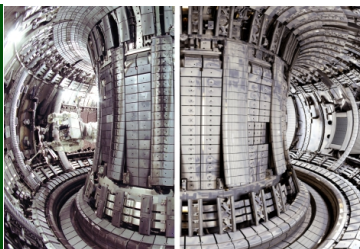
man-made plasmas are bounded by confining solid walls

dusty plasmas



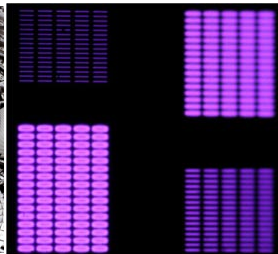
A. Melzer

fusion plasmas



Schorn, FZ Juelich

microdischarges



Kulsreshath, PSST (2014)

- plasma interacts with solids
- ion-, radical-, and **electron-solid interaction** $\rightarrow \alpha, Y_e^*, (S_e, R_e, Y_e \rightarrow S, R, Y)$
- electron impact energies depend on plasma context
- focus of presentation: **very low electron impact energies (< 50 eV)**

Solid-state-based microdischarges

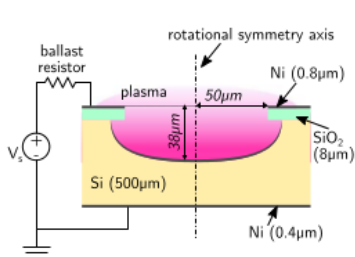
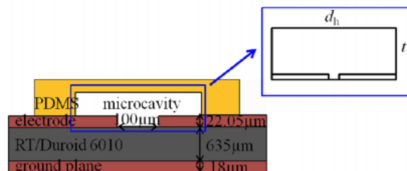


Figure 1. Schematic of a single silicon based MHCD reactor produced by MEMS manufacturing technology.

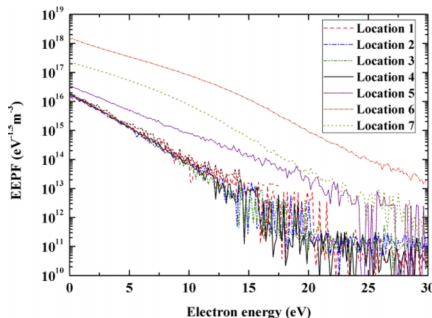
S. Iseni *et al.*, PSST. **28**, 065003 (2019)

- V_s typically a few 100 eV
- plenty of e^- interacting with solid boundaries at $E < 50$ eV
- need R_e , S_e , and Y_e for **very low impact energies** and variety of materials



J. Tang *et al.*, AIP Adv. **6**, 045016 (2016)

location 1–4 along electrode



See also, J. Choi *et al.*, IEEE Trans. Plasma Science **35**, 1274 (2007)

Very low electron impact energies – challenge

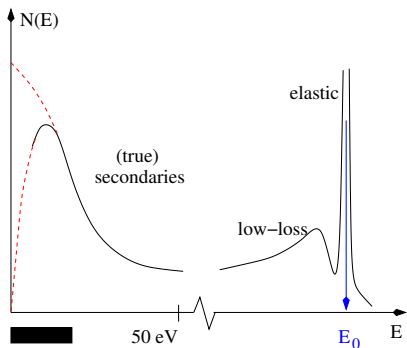
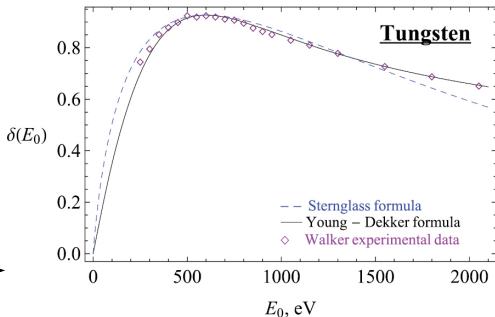


Figure 5 from P.Tolias 2014 Plasma Phys. Control Fusion 56 123002

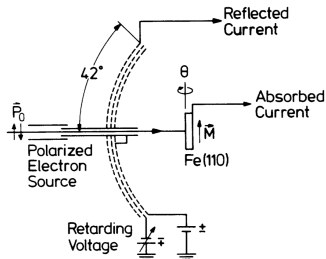


From P. Tolias, PPCF **56**, 123002 (2014).

- $E_0 < 50 \text{ eV} \Rightarrow$ true secondaries and inelastically scattered primaries **not clearly separable**
- **solid state effects matter** (surface potential, electronic structure)
- established empirical formulae for $\delta(E_0)$ [$\rightarrow Y(E_0)$] not applicable

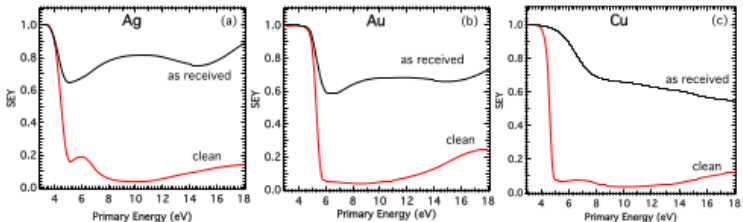
$\Rightarrow Y, R,$ and S have to be calculated and measured

Measuring secondary electron emission yields – beam experiments



- sophisticated electron spectroscopy and vacuum equipment
- angle and energy resolved measurements
- control over surface quality (single crystals)
- **but: not applicable to plasma environment**

M. S. Hammond *et al.*, PRB **45**, 6131 (1992)



Focus on “clean” (well characterized) samples! L. A. Gonzalez *et al.*, AIP Advances **7**, 115203 (2017)

Measuring electron sticking coefficients – electric probe experiments

V. I. Demidov, S. F. Adams, I. D. Kaganovich, M. E. Koepke, I. P. Kuriyandskaya, Phys. Plasma **22**, 104501 (2015)

1 & 2=clean & dirty Mo; 3=dirty Mo (Bronshtein), 4=Cu (Cimino)

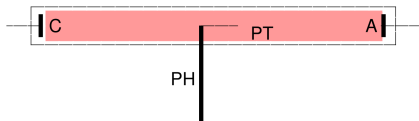
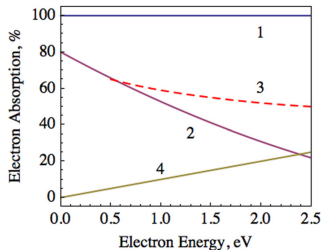
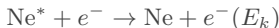


FIG. 3. Schematic of the experimental device. A glass tube has a diameter of 35 mm and length of 30 cm with cold cathode (C) and anode (A). A probe tip (PT) is situated along the tube axis, and probe holder (PH) is perpendicular to the tube axis.



- Ne afterglow plasma, **heavy particle collisions generate e^- beam with E_k**



- probe current modified by electron reflection $I_d(V) = I_c(V)G(eV)$

$$G(U) = 2 \int_0^{\pi/2} d\theta \sin \theta \cos \theta S_e(E - U, \theta)$$

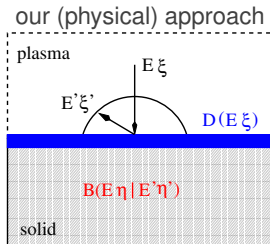
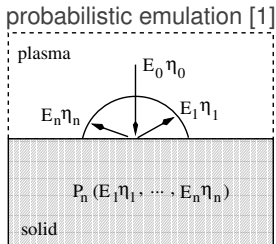
- possibility to extract $S_e = 1 - Y_e$
- **interesting operando method, but how well characterized are surfaces?**

Computational approach

Before we get started

Connection to plasma modeling

- electron-solid interaction encapsulated in BC
- two fundamentally different approaches to do that



- **input:** $Y_e = Y_{el} + Y_{inelastic} + Y_{ts}$, dY_e/dE
- **output:** $P_n \Leftrightarrow$ **prob. for event in particle-based simulation**
- **input:** microphysics of interface (elementary excitations, $E(\vec{k})$, ...)
- **output:** Y_e , $dY_e/dE \Rightarrow$ **surface scattering kernel=BC for e^- BE**
 $f_e^> = R_e \circ f_e^<$

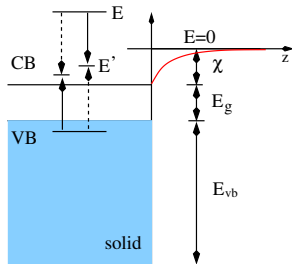
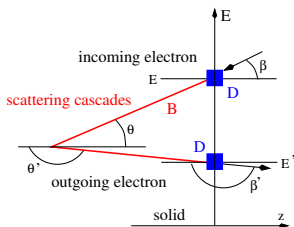
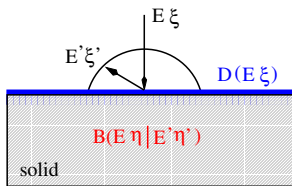
[1] M. A. Furman and M. T. F. Pivi, Phys. Rev. Spec. Topics - Accelerator and Beams, **5**, 124404 (2002)

Stages of development of our (physical) approach

- **initially, we applied our approach to dielectrics with $\chi > 0$ [1]**
 - conditional probability construction to obtain B from Q
 - step potential, scattering on optical phonons and surface defects
 - $E < E_g \Rightarrow$ no impact ionization
 - linearized embedding equation for $Q \Rightarrow$ algebraic recursion relations
- **then, we generalized our approach substantially and applied it to metals [2]**
 - still conditional probability construction for B
 - image step with Bragg scattering, energy gaps at surface
 - ei, ep, ee, and scattering on surface defects
 - no linearization of embedding equation but quasi-isotropic approximation
 - \Rightarrow set of linear integral equations instead of algebraic equations
- **now, we applied it to semiconductors with $\chi > 0$ [3]**
 - conditional probability construction for B abandoned
 - image step, ei, ep, and impact ionization (hence, $E > E_g$ now allowed)
 - no linearization and no quasi-isotropic approximation
 - \Rightarrow full embedding equation for $Q \Rightarrow$ Ricatti and a set of Sylvester equations

[1] FXB and H. Fehske, PRL **115**, 225001 (2015); ibid. PPCF **59**, 014011 (2017); [2] ibid. JAP **131**, 113302 (2022); [3] FXB and F. Willert, arXiv:2309.00534 and submitted (2023).

Calculational approach – cartoon



Notation: scattering from $(E, \eta) \rightarrow (E', \eta')$

model for semiconductor

So far: chemically clean surfaces;
 surface chemistry due to plasma could be buried in D

Emission yield for structurally perfect surface

$$Y(E, \xi) = \int_0^E dE' \int_0^1 d\xi' R(E, \xi|E', \xi')$$

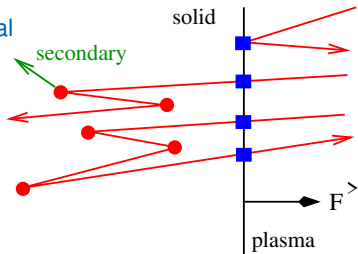
$$\underbrace{R(E, \xi|E', \xi')} = R(E, \xi)\delta(E - E')\delta(\xi - \xi') + \Delta R(E, \xi|E', \xi')$$

electron surface scattering kernel

Calculational approach – electron surface scattering kernel

Electron-solid interaction

- **qm transmission through interface potential**
electron mass mismatch
 $V(z)$ across interface
energy gaps
- **scattering cascades inside solid**
elastic & inelastic processes
electron multiplication
band structure
- **electron surface scattering kernel R** \Rightarrow emission yield Y & BC for BE



$$F^>(E', \xi') = \int_0^\infty dE \int_0^1 d\xi F^<(E, \xi) R(E, \xi | E', \xi')$$

$$R(E, \xi | E', \xi') = R(E, \xi) \delta(E - E') \delta(\xi - \xi') + \Delta R(E, \xi | E', \xi')$$

$$\Delta R(E, \xi | E', \xi') = \frac{E'}{E' + \chi} \frac{\xi'}{\eta'} \rho(E') \Theta(E - E') D(E, \xi) B(E, \eta(\xi) | E', \eta(\xi')) D(E', \xi')$$

Computational approach – alternative expression for Y [1]

Emission yield $Y(E, \xi)$ for an electron hitting perfect ($C = 0$) or irregular ($C \neq 0$) surface with (E, ξ)

- **irregular** surface $\rightarrow \int_0^1 d\xi'(\dots)$
- **qm transmission** through surface potential $\rightarrow \mathbf{D}(\mathbf{E}, \xi) = \mathbf{1} - \mathbf{R}(\mathbf{E}, \xi)$
- **internal scattering cascade** $\rightarrow B(E\eta|E'\eta') \rightarrow$ invariant embedding principle

$$Y(E, \xi) = 1 - S(E, \xi)$$

$$S(E, \xi) = \frac{D(E, \xi)}{1 + C/\xi} [1 - \mathcal{E}(E, \xi)] + \frac{C/\xi}{1 + C/\xi} \int_0^1 d\xi' D(E, \xi') [1 - \mathcal{E}(E, \xi')]$$

$$\mathcal{E}(E, \xi) = \int_{\eta_{\min}(E)}^1 d\eta' \int_{E_{\min}(\eta')}^E dE' \rho(E') B(E\eta(\xi)|E'\eta') \bar{D}(E', \xi(\eta'))$$

$$\bar{D}(E, \xi) = \frac{D(E, \xi)}{1 + C/\xi} + \frac{C/\xi}{1 + C/\xi} \int_0^1 d\xi' D(E, \xi') \quad , \quad C \sim |M|^2 n_{\text{surface defects}}$$

Limiting cases: $C \rightarrow 0$ (perfect) and $C \rightarrow \infty$ (very irregular)

[1] FXB and H. Fehske, PRL **115**, 225001 (2022); ibid. PPCF **59**, 014011 (2017)

Computational approach – capabilities/options

overall

- irregular surface \Leftrightarrow (elastic) surface defects

surface transmission function D

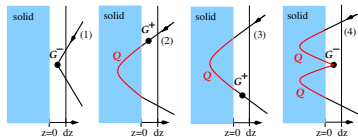
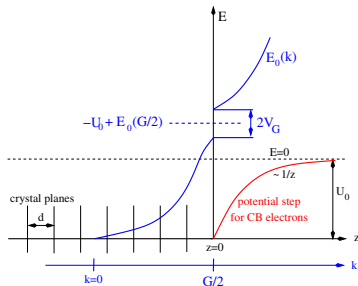
- image step plus Bragg gap (two band model)

bulk transition rates W^\pm

- (statically screened) el-el scattering
→ two final states
- (quasi-elastic) electron-phonon scattering
- incoherent elastic scattering by ion cores
→ pseudo-potentials for ion cores

invariant embedding equations for $Q \Rightarrow B$

- decoupling of E and $\eta \Leftrightarrow$ quasi-isotropic approximation (QIA) [1]
- now: numerical solution without QIA [2]**



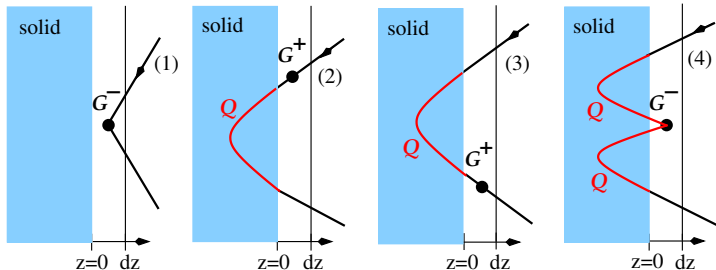
$\bullet \hat{=} G^+$ or G^- with $G^\pm = W^\pm / \eta v$

[1] FXB and H. Fehske, JAP **131**, 113302 (2022); [2] FXB and F. Willert, arXiv:2309.00534 and submitted (2023).

Computational approach – invariant embedding principle

Dashen (1964): Adding an infinitesimally thin layer of the same material to a **thick surface** should not alter $Q(E\eta|E'\eta')$.

R. Dashen, Phys. Rev. **134**, A1025 (1964)



• $\hat{=}$ G^+ or G^- with $G^\pm = W^\pm/\eta v$

$$dQ = \left\{ G^- + G^+ \circ Q + Q \circ G^+ + Q \circ G^- \circ Q - \left(\frac{\Pi}{\eta} + \frac{\Pi'}{\eta'} \right) Q \right\} dz = 0$$

$$(A \circ B)(E\eta|E'\eta') = \int_{E'}^E dE'' \int_0^1 d\eta'' \rho(E'') A(E\eta|E''\eta'') B(E''\eta''|E'\eta')$$

Calculational approach – kernels

Scattering rates and the like – **Golden Rule** $(E, \eta) \rightarrow (E', \eta')$

$$G^\pm(E\eta|E'\eta') = \frac{W^\pm(E\eta|E'\eta')}{v(E)\eta} \quad \Pi(E) = \frac{\Gamma(E)}{v(E)}$$

$$W^\pm(E\eta|E'\eta') = \int_0^{2\pi} d\phi W(E\eta|E'\eta'; \phi)$$

$$\Gamma(E) = \int_{-\chi}^E dE'' \int_0^1 d\eta'' \rho(E'') [W^+(E\eta|E''\eta'') + W^-(E\eta|E''\eta'')]$$

$$W^\pm(E\eta|E'\eta') = W_{e1}^\pm(E\eta|E'\eta') + W_{ee}^\pm(E\eta|E'\eta')$$

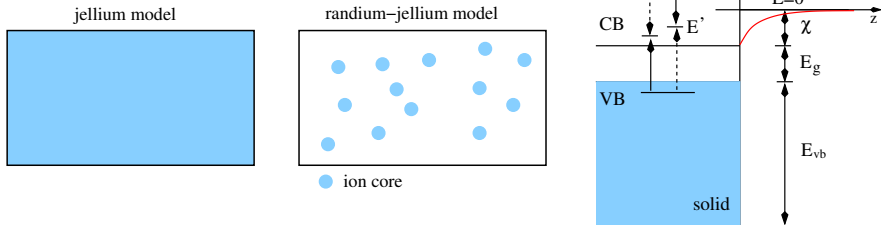
Embedding equation for $Q(E\eta|E'\eta')$ to be solved

$$S \circ Q + Q \circ S = G^- + G^+ \circ Q + Q \circ G^+ + Q \circ G^- \circ Q$$

$$S(E, \eta|E', \eta') = \frac{\Pi(E)}{\eta} \delta(E - E') \delta(\eta - \eta')$$

Computational approach – radium jellium model for ion cores [1]

- incoherent scattering on randomly distributed ion cores
- quasi-elastic electron-phonon scattering
- impact ionization across bulk energy gap



$$W_{\text{elastic}}^{\pm}(E, \eta | E', \eta') = W_{\text{ep}}^{\pm}(E, \eta | E', \eta') + W_{\text{eic}}^{\pm}(E, \eta | E', \eta')$$

$$W_{\text{ep}}^{\pm}(E, \eta | E', \eta') = \frac{M^2}{(2\pi)^2} [1 + 2n_B(\omega_{\text{LO}})] \delta(E - E') \Theta(E_{\text{th}} - E)$$

$$W_{\text{eic}}^{\pm}(E, \eta | E', \eta') = \frac{1}{(2\pi)^2 n_{\text{ion}}} \langle |U_{\text{PS}}(g^{\pm})|^2 \rangle_{\Phi} \delta(E - E') \Theta(E - E_{\text{th}})$$

$$W_{\text{impact}}^{\pm}(E, \eta | E', \eta') = \mathcal{W}(E, T, 1 | E', T', \pm 1) \quad \text{Monte Carlo integration required}$$

[1] For details see, FXB and F. Willert, arXiv:2309.00534 and submitted (2023).

Computational approach – numerics

Adopting Shimizu and Mizuta's approach of solving embedding-type equations in nuclear transport theory. A. Shimizu and H. Mizuta, J. Nucl. Sci. Technol. **3**, 57 (1966)

(i) Discretization of energy space

$$A_{nm}(\eta|\eta') = \int_n dE \int_m dE' A(E, \eta|E', \eta') f_n(E) \quad , \quad f_n(E) = 1/\Delta E_n$$

⇒ Ricatti/Sylvester equations for $Q_{nm}(\eta|\eta')$

$$S_n * Q_{nn} + Q_{nn} * S_n = G_{nn}^- + Q_{nn} * G_{nn}^- * Q_{nn} \\ + G_{nn}^+ * Q_{nn} + Q_{nn} * G_{nn}^+$$

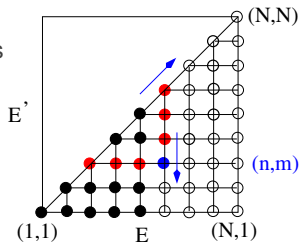
$$S_n * Q_{nm} + Q_{nm} * S_m = K_{nm}^-$$

(ii) Realizing Volterra-type structure of energy integrals

⇒ sampling energy space such that $Q_{kr}(\eta|\eta')$ inside K_{nm}^- known from previous step

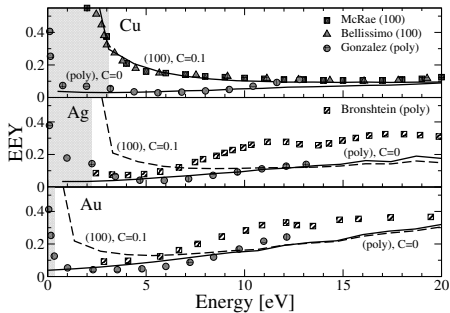
$$K_{nm}^- = \dots + C_{nm}^- + \dots$$

$$C_{nm}^- = \sum_{l=m+1}^{n-1} \sum_{p=m}^l Q_{nl} * G_{lp}^- * Q_{pm}$$



Numerical results

Results – metals (Cu, Ag, Au)



- quasi-isotropic approximation (not discussed in this talk)

FXB and H. Fehske, JAP **131**, 113302 (2022)

- **cond. prob. construction**

$$\begin{aligned}
 B &= B(E\eta|E'\eta') \\
 &= \frac{(2Q_{ee} + Q_{ei})(E\eta|E'\eta')}{\int_{-\chi}^E d\bar{E} \int_0^1 d\bar{\eta} \rho Q(E\eta|\bar{E}\bar{\eta})}
 \end{aligned}$$

- successful also for W and Al

- **for Cu (100) nearly perfect agreement** between theory and experiment

E. G. McRae and C. W. Caldwell, Surf. Science **57**, 77 (1976)

A. Bellissimo, PhD thesis, Università degli Studi Roma Tre (2019), <https://doi.org/10.5281/zenodo.3924096>

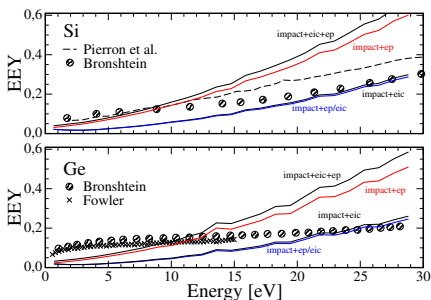
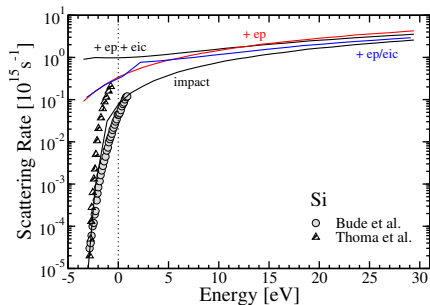
- for $E > 2$ eV Gonzalez data for Cu, Ag, and Au [2] **fairly well reproduced**

L. A. Gonzalez *et al.*, AIP Advances **7**, 115203 (2017)

Despite quantitative success, cond. prob. construction problematic.

Wrong limit for vanishing interface potential; Flaw of construction perhaps compensated by QIA?; Under investigation.

Results – semiconductors (Si, Ge) – $Y(E, \xi = 1)$

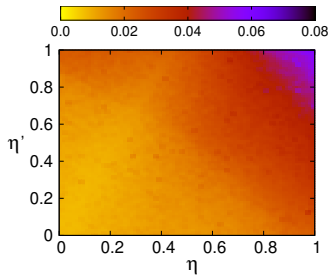
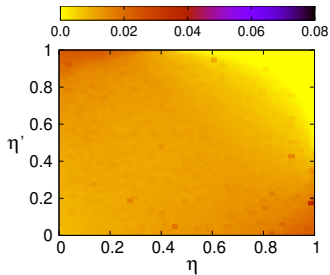
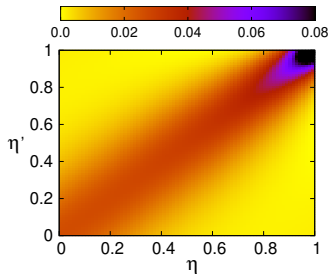
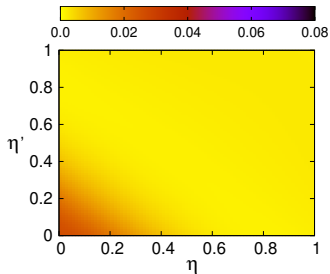


- **no cond. probability construction:** $B(E\eta|E'\eta') = Q(E\eta|E'\eta')$
- **semi-empirical description of solid** (band structure, scattering, screening)
 - parabolic VB and CB with $m_{CV}^* = m_{VB}^* = m_e$
 - adhoc ep/eic when $\lambda_{dB} \sim a_L$, that is, at $E_{th} = -\chi + (2\pi/a_L)^2 \sim 0$ eV
 $E < E_{th}$: impact+ep; $E > E_{th}$: impact+eic
 - screening of ee, eic, and ep (bond vs. atomic like VB charge)
- experimental data reasonably well reproduced; **need more measurements!**
 - no tunable parameters!

Results – semiconductors (Si) – $W^\pm(E\eta|E'\eta')$ – angle dependence

$W^- : E = 28.8 \text{ eV}, E' = 28.8, 1.8 \text{ eV}$

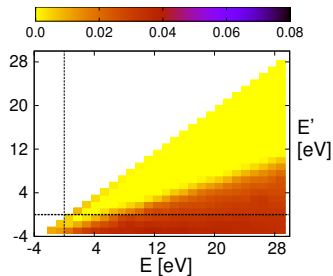
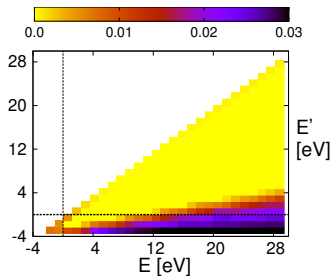
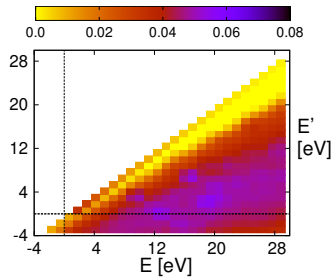
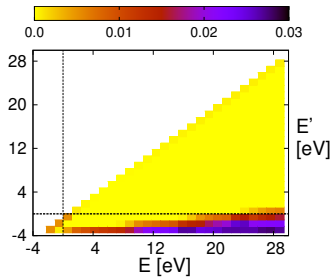
$W^+ : E = 28.8 \text{ eV}, E' = 28.8, 1.8 \text{ eV}$



Results – semiconductors (Si) – $W^\pm(E\eta|E'\eta')$ – energy dependence

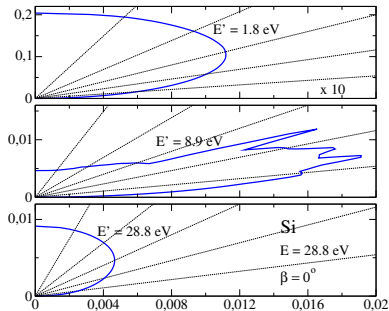
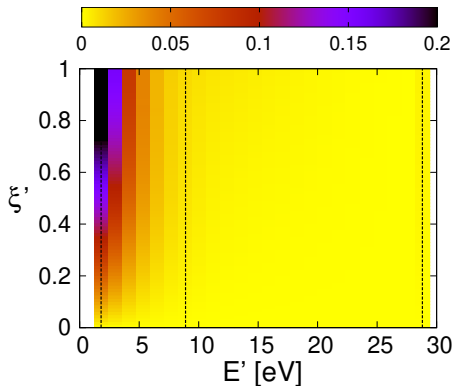
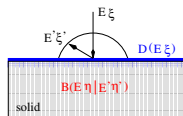
$W^- : \eta = 1, \eta' = 0.75, 0.24$

$W^+ : \eta = 1, \eta' = 0.75, 0.24$



Results – semiconductors (Si) – $R(E, \xi|E', \xi')$

- primary e^- : $\xi = 1$ and $E = 28.8 \text{ eV}$

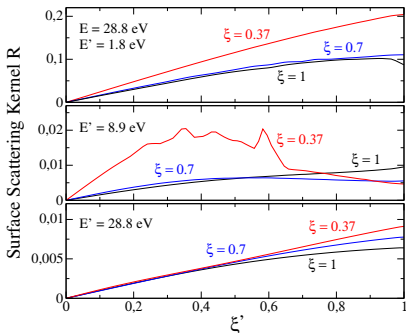
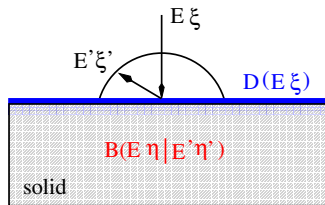


- $R(E, \xi|E', \xi')$ can be obtained for any E and ξ
 \Rightarrow BC for BE which takes solid's electron microphysics into account

$$F^>(E', \xi') = \int_0^\infty dE \int_0^1 d\xi F^<(E, \xi) R(E, \xi|E', \xi')$$

Conclusion

Take home messages



- embedding approach for $Q(E, \eta | E', \eta')$ used to calculate surface scattering kernel [1] and not only emission yield [2]

[1] FXB and F. Willert, arXiv:2309.00534 and submitted (2023); [2] FXB and H. Fehske, JAP **131**, 113302 (2022); ibid. PPCF **59**, 014011 (2017); ibid. PRL **115**, 225001 (2015).

- embedding equation for Q solved without approximation
 - **transport problem for $Q(E \eta | E' \eta')$ under control**
 - **focus now on semi-empirical description of solid**
 - **operando diagnostics of plasma-exposed surfaces required**

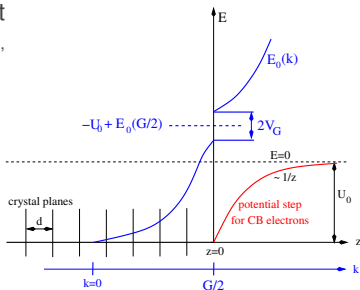
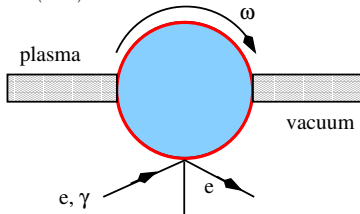
Operando surface diagnostics – How and why?

Only few experimental data for Y at $E < 20$ eV \Rightarrow **measurements required!**

- free-standing, well-characterized surfaces – would be good
- **plasma-exposed surfaces** – better

Spinning wall setup \rightarrow beam experiment

J. Guha, Y.-K. Pu and V. M. Donnelly, J. Vac. Sci. Technol. A **25**, 347 (2007)



- electronic structure of plasma-exposed surface (photoelectron spectroscopy)
potential barriers $\rightarrow U_0$, energy gaps $\rightarrow 2V_G$
- chemical and structural composition (Auger spectroscopy)
- measuring electron reflection and emission yields would be really great!